

# Investigating Data Assimilation Methodologies for Improved Swell Prediction Accuracy

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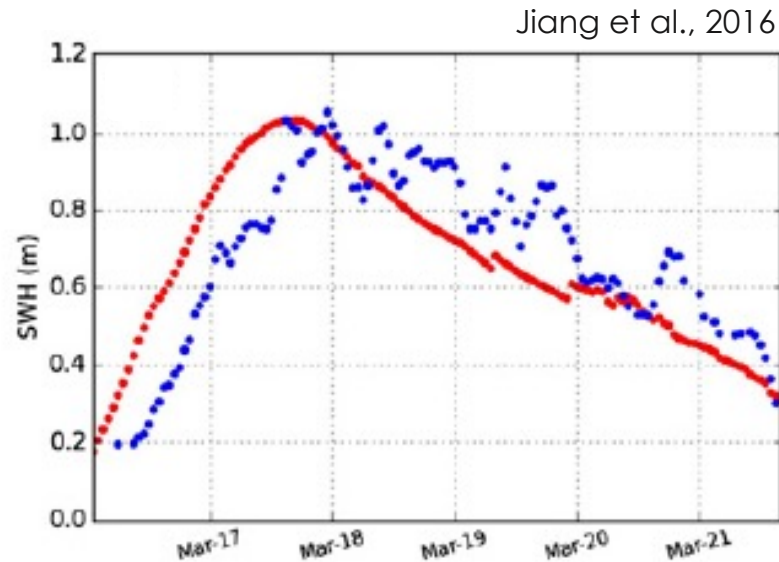
# Southern Ocean Swell

Southern Ocean is a major swell generation region for much of the world's oceans



# Swell at Northwest Shelf

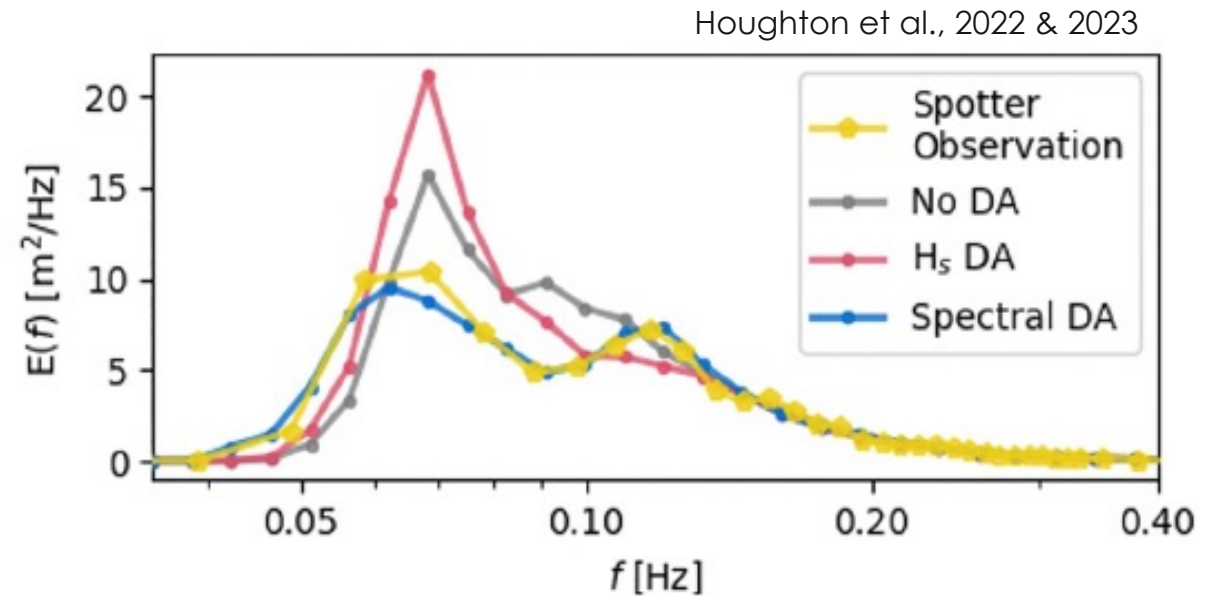
Inaccuracies in swell prediction



Caused by limitations in:

- Observational data,
- Theoretical assumptions, and
- Their implementation.

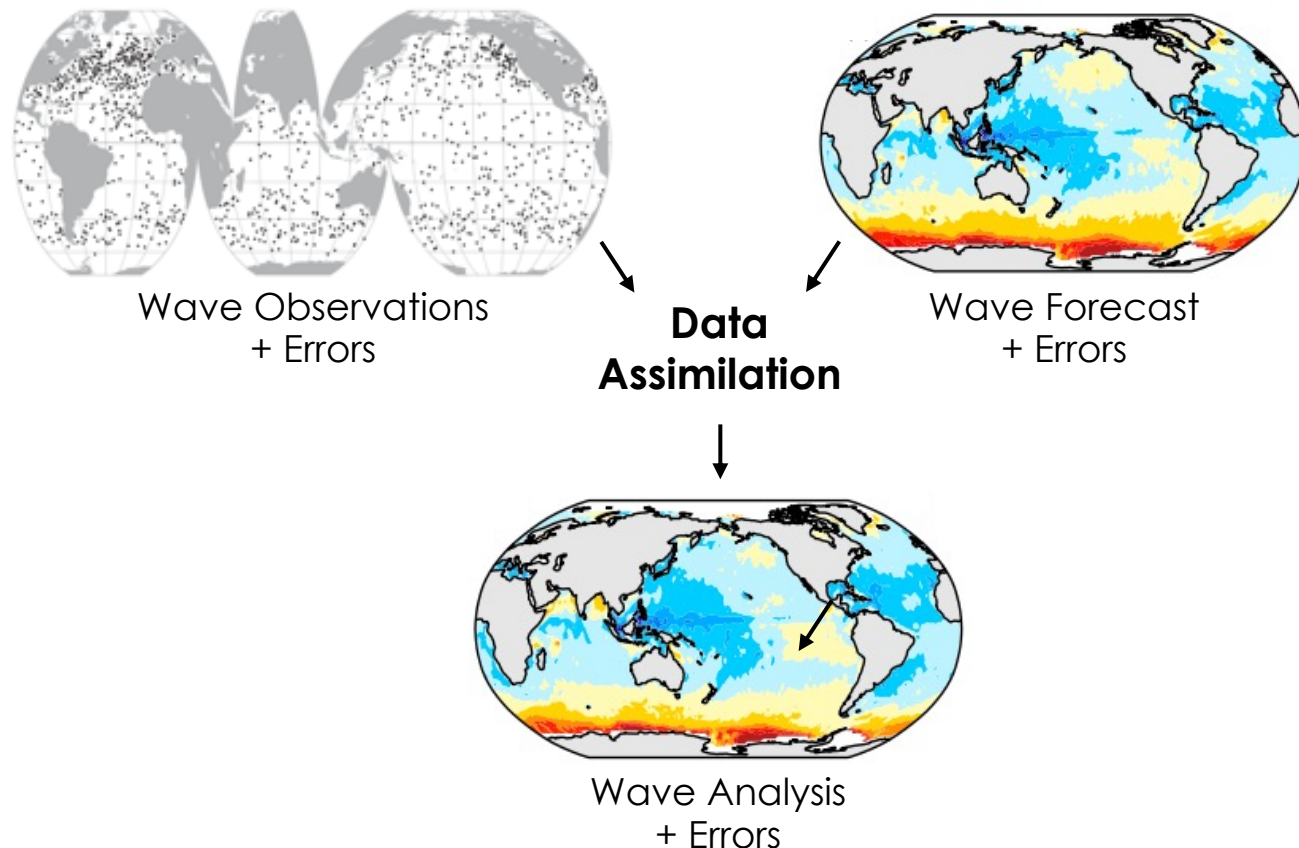
Incorporating wave observations through data assimilation can reduce uncertainty in swell predictions



# Data Assimilation



Australian Government  
Bureau of Meteorology



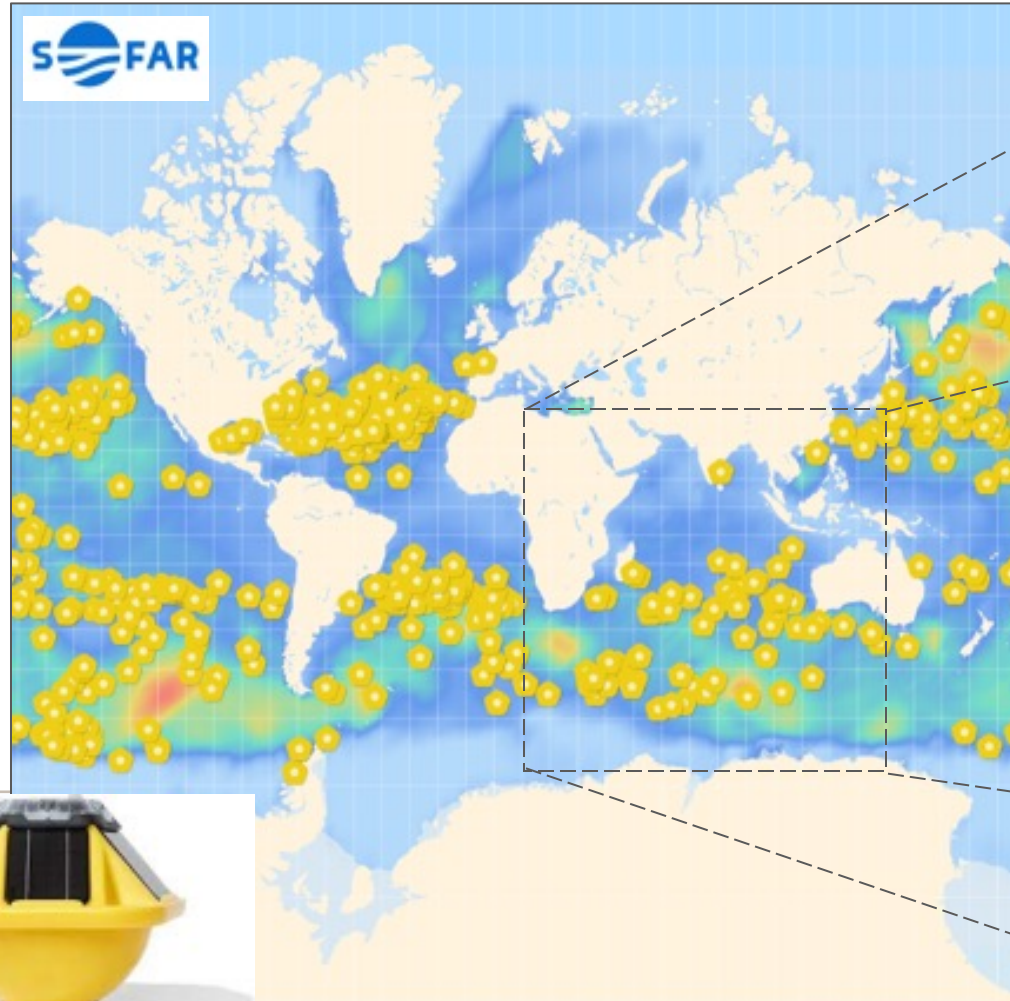
Model	Name	Data Assimilation
Atmospheric	ACCESS	4D VAR
Ocean	OceanMAPS	Ensemble KF
Wave	AUSWAVES	No DA

DA in operational wave models (e.g., ECMWF and MeteoFrance): reliant on bulk parameters.

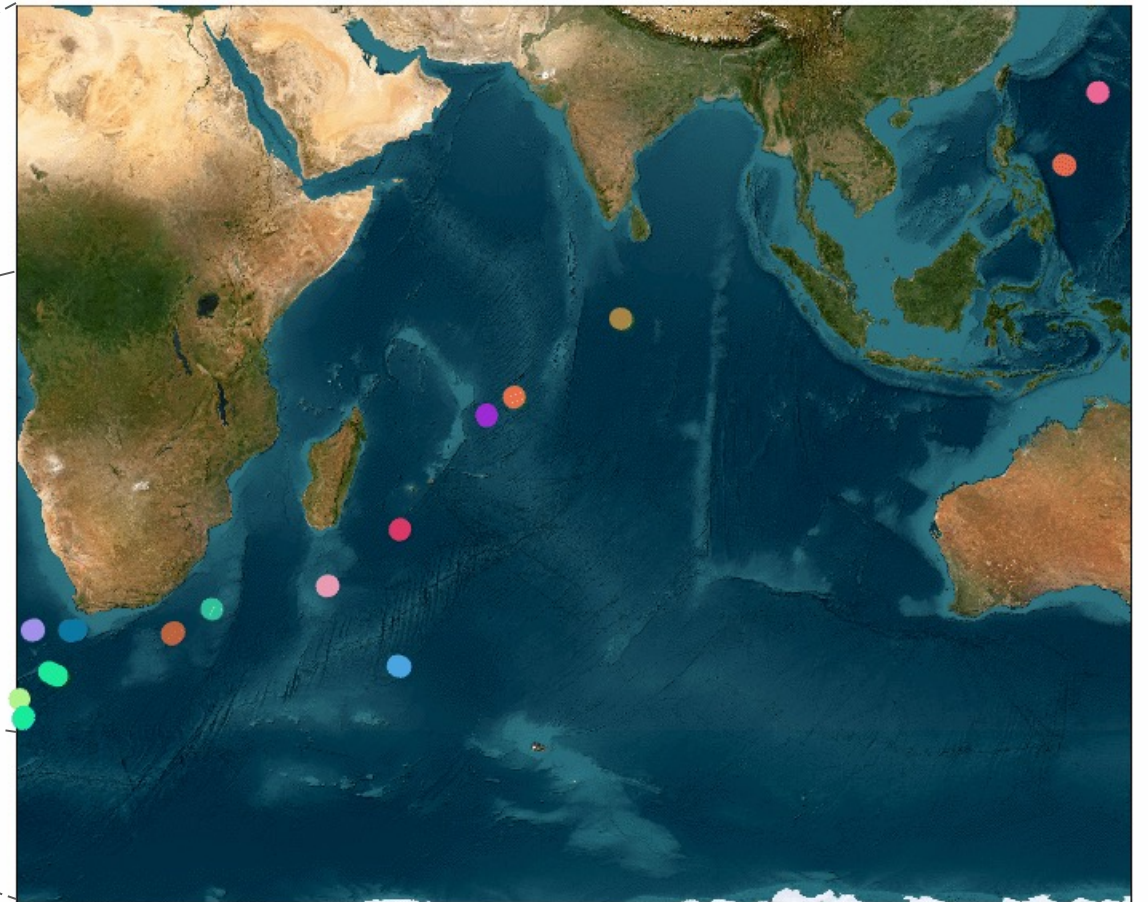
## Objective:

Develop spectral wave assimilation methods to improve the prediction capabilities of operational forecasts with a focus on swells.

# SOFAR's Network of Spotter Buoys



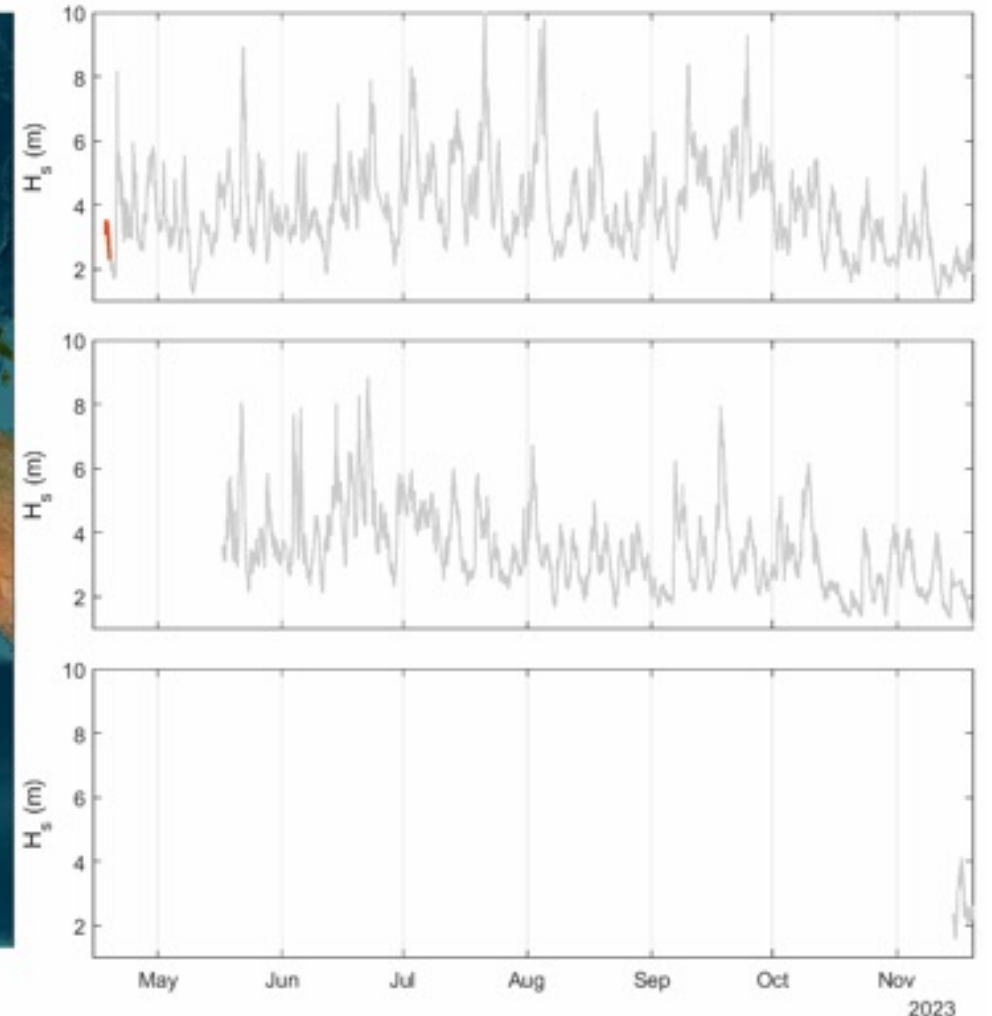
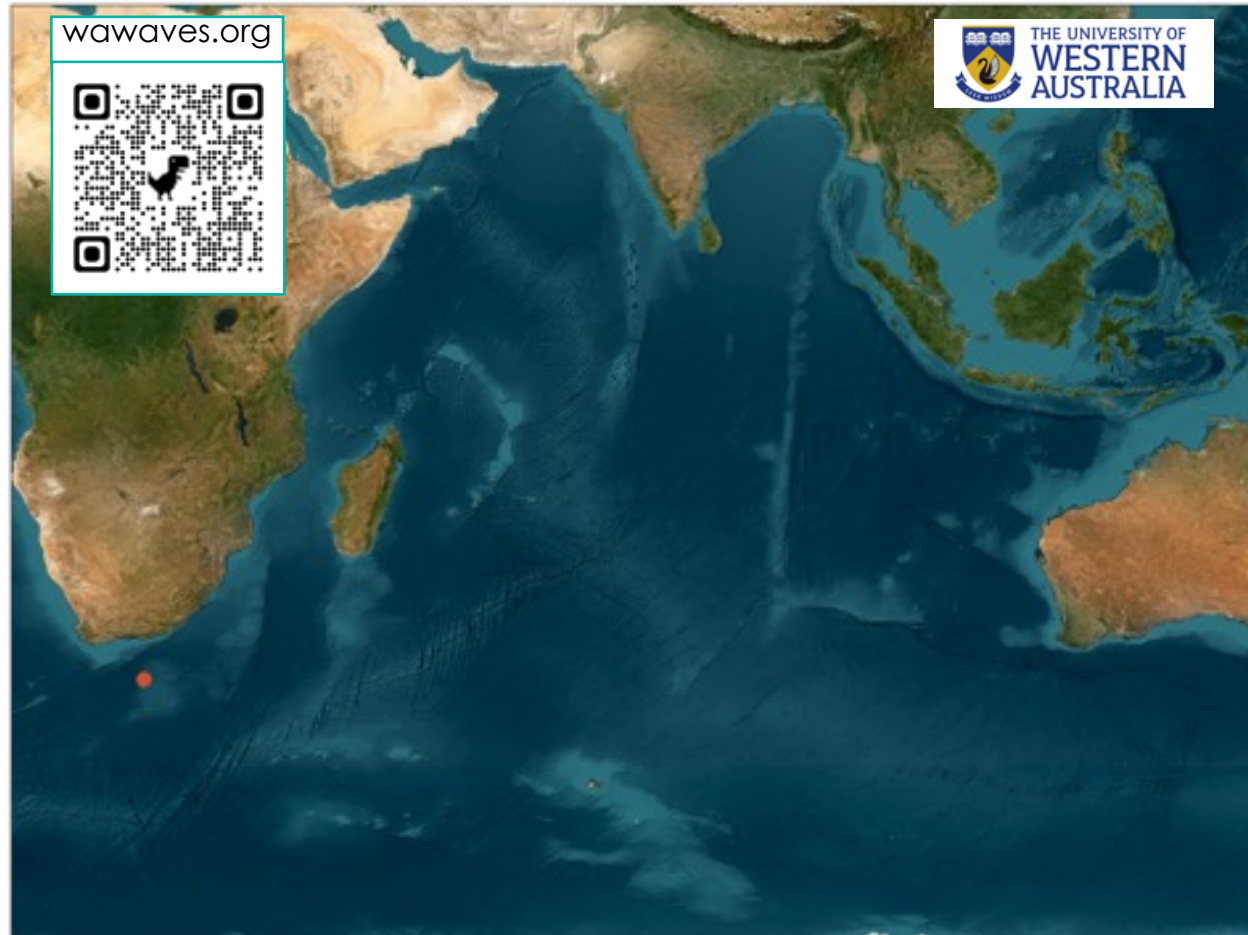
15 Jan. 2021

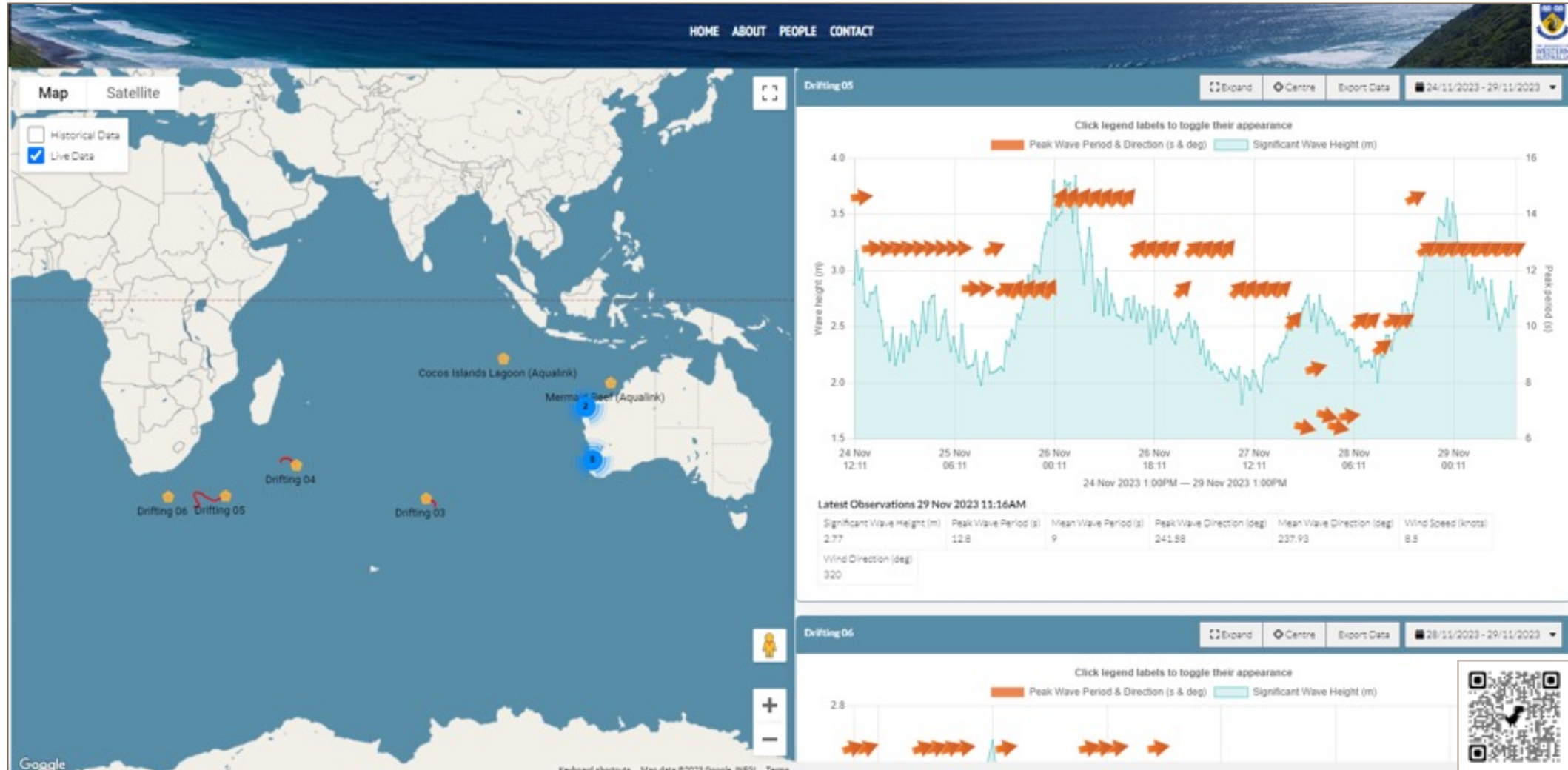


# Observational Data



18 Apr. 2023





# Other Observational Data



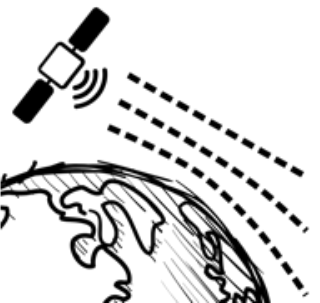
## Satellite Observations

Mean parameters:

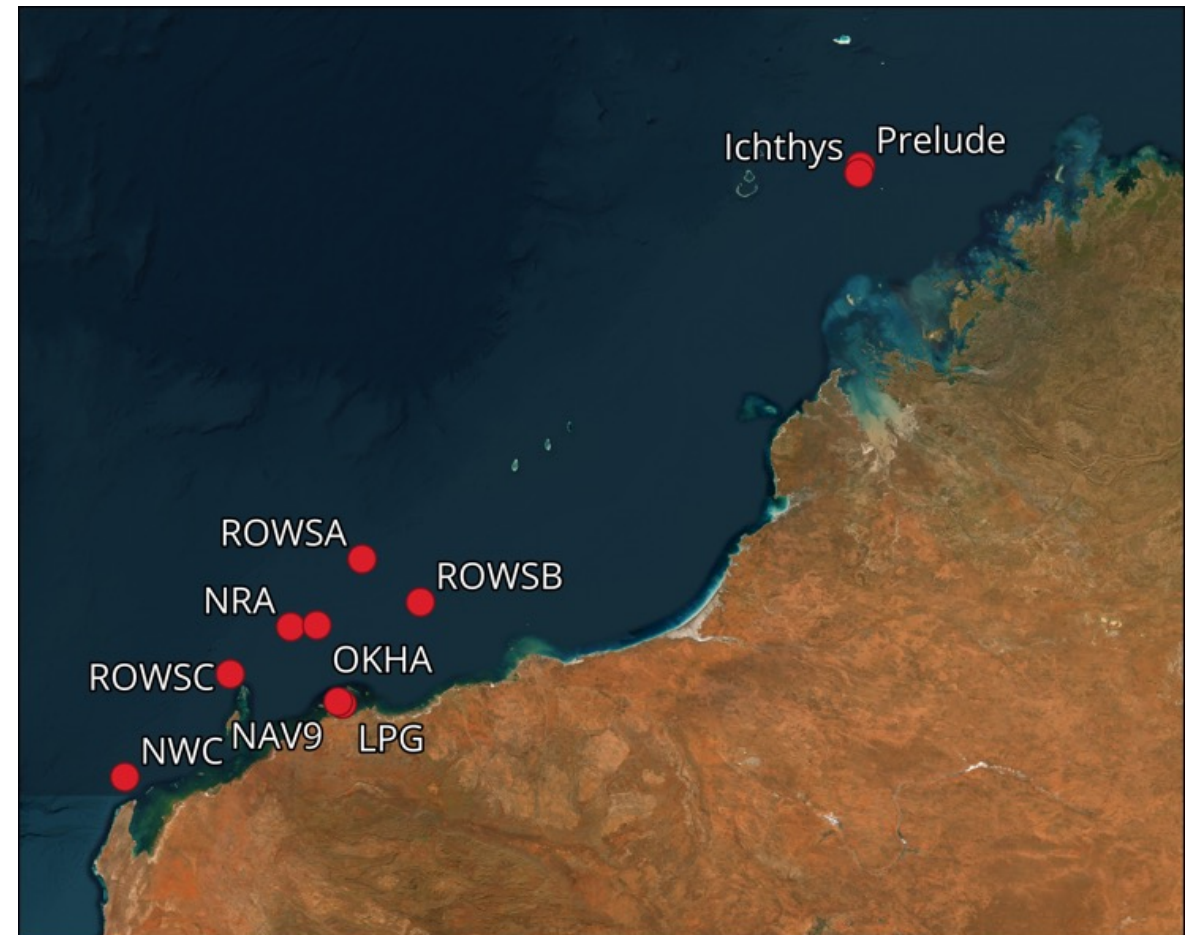
Altimeter

Wave Energy Spectra:

Synthetic Aperture Radar (SAR), and Chinese-French Oceanography Satellite (CFOSAT).



## Industry Operated Buoys at NWS





# AUSWAVE-G3



**Australian Government**  
**Bureau of Meteorology**

## A multiple-resolution global wave model

Stefan Zieger and Diana J. M. Greenslade

May 2021

WaveWatch-III v6.07 wave model



Wind:  
ACCESS-G3



Current:  
OceanMAPS

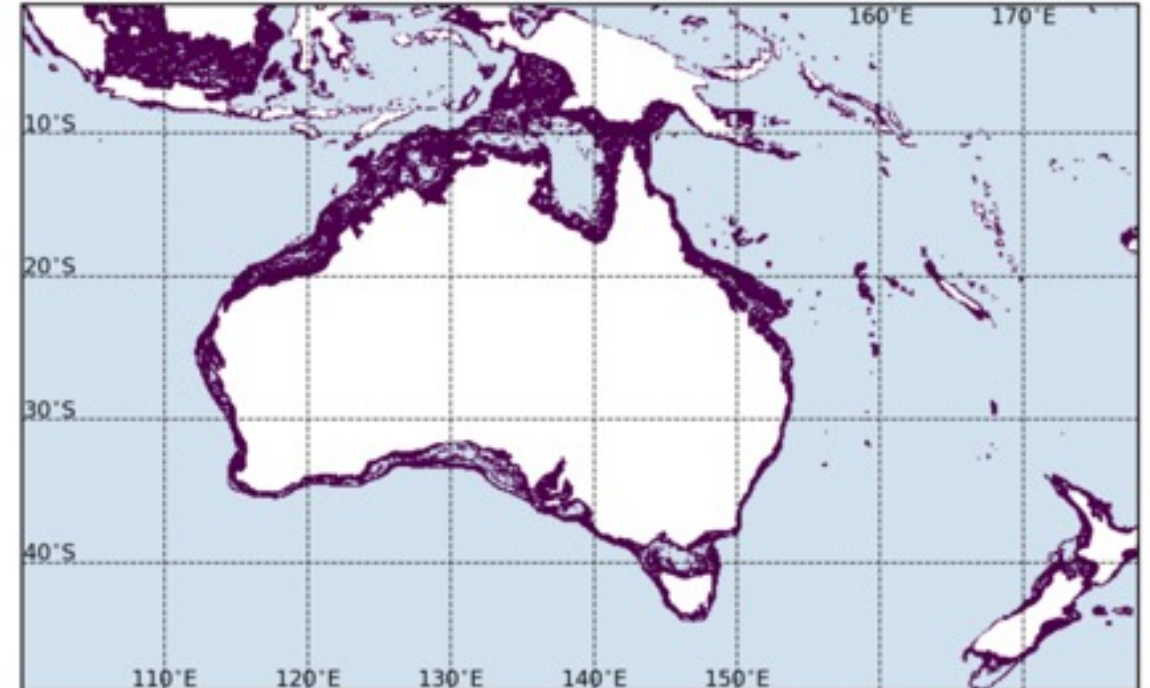
Spectral resolution:

30 direction bins

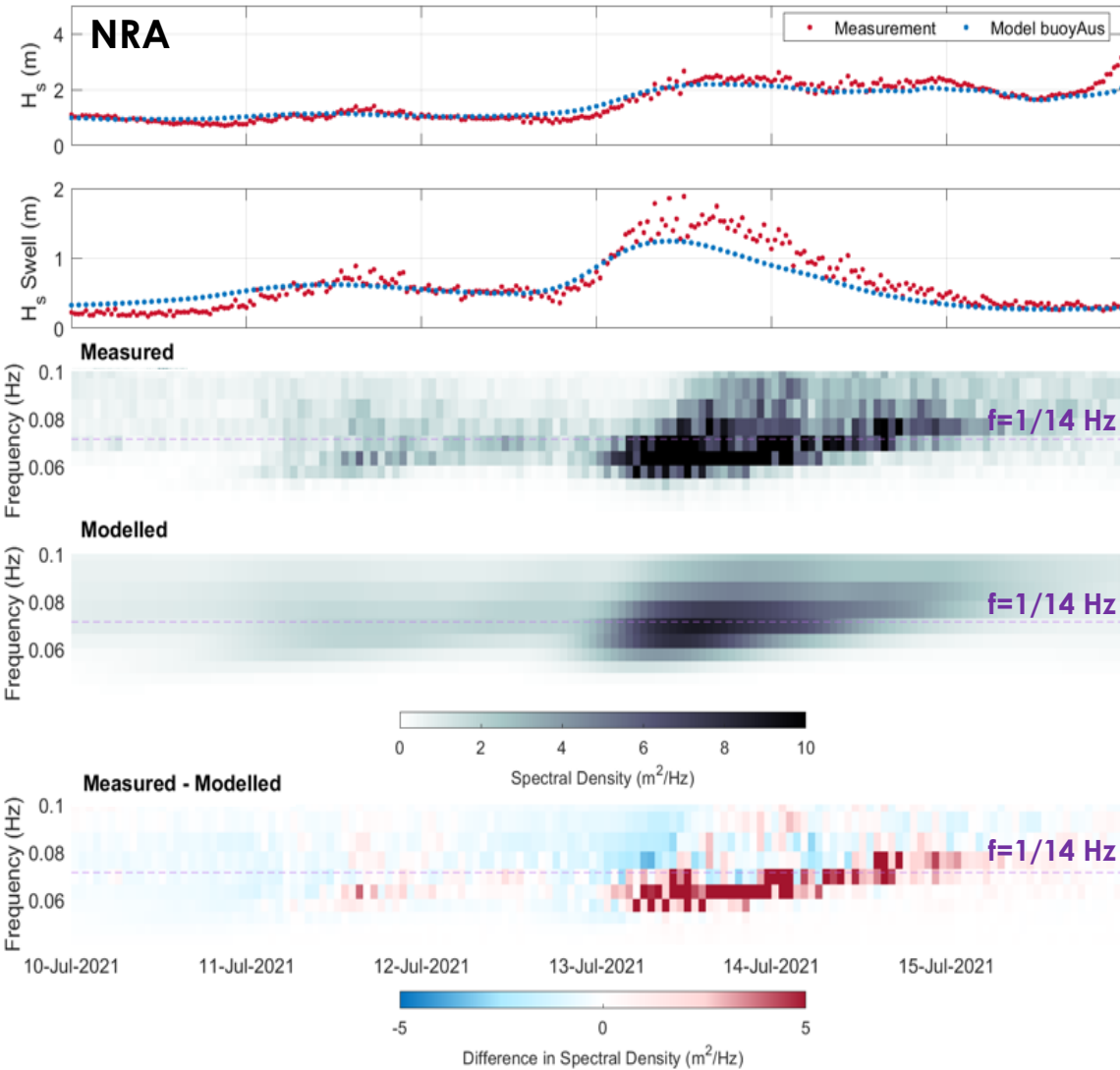
28 frequency bins (0.0412Hz - 0.5401Hz)

Spatial resolution:

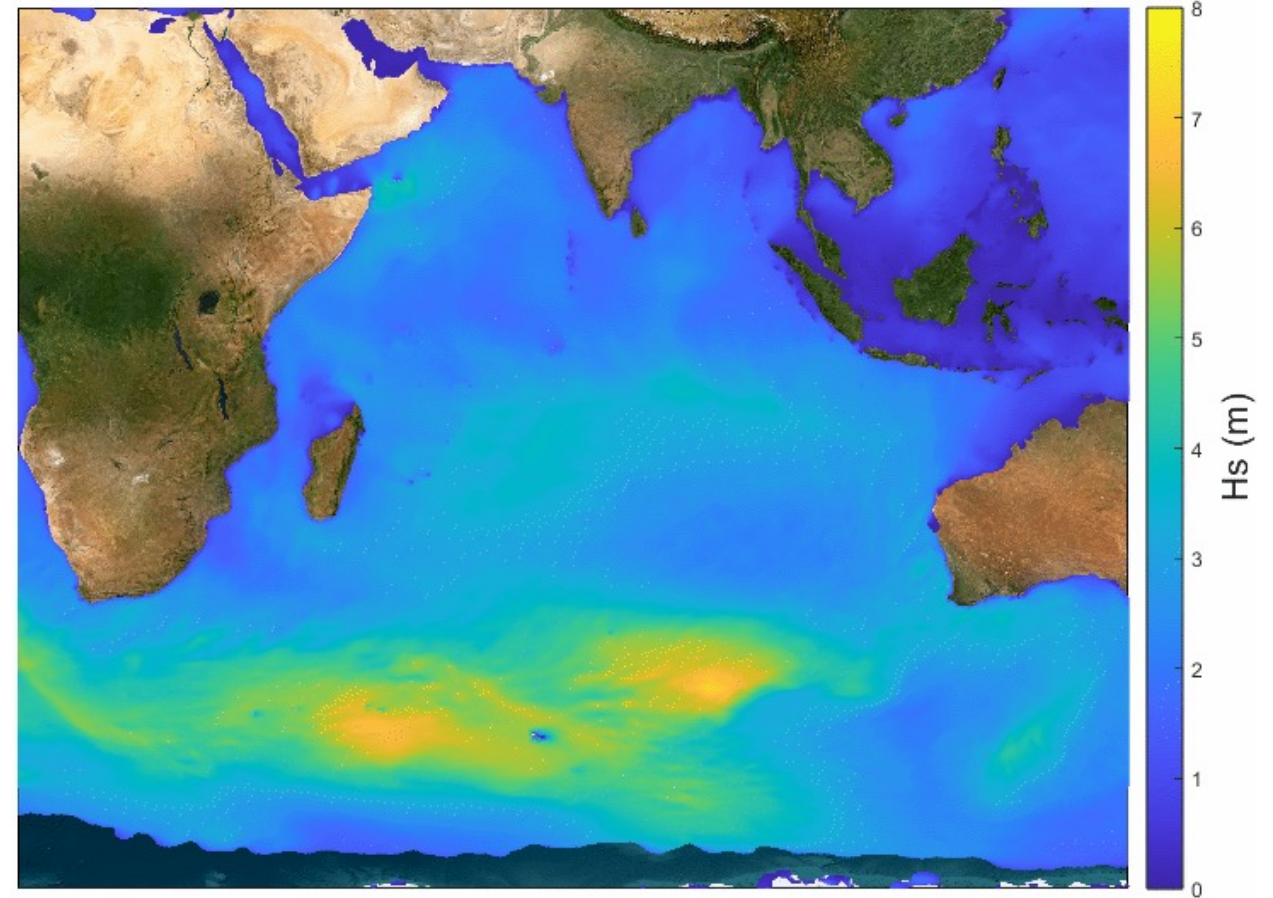
~12km global with ~6km sub-grid



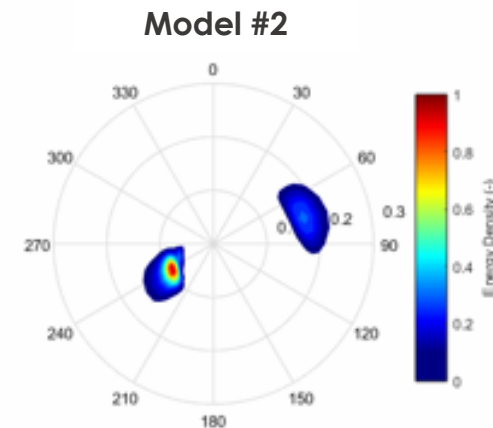
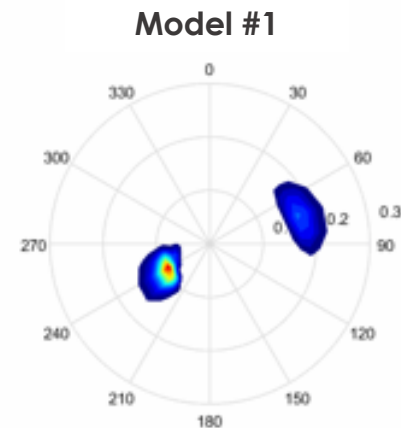
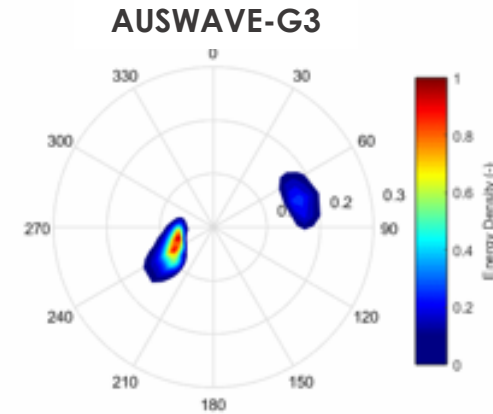
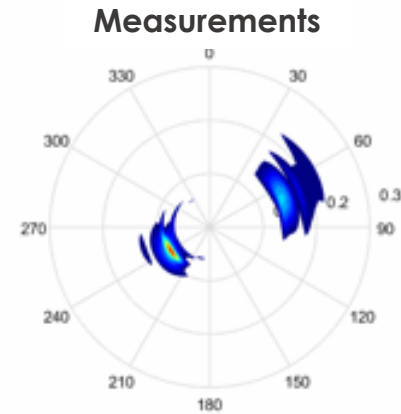
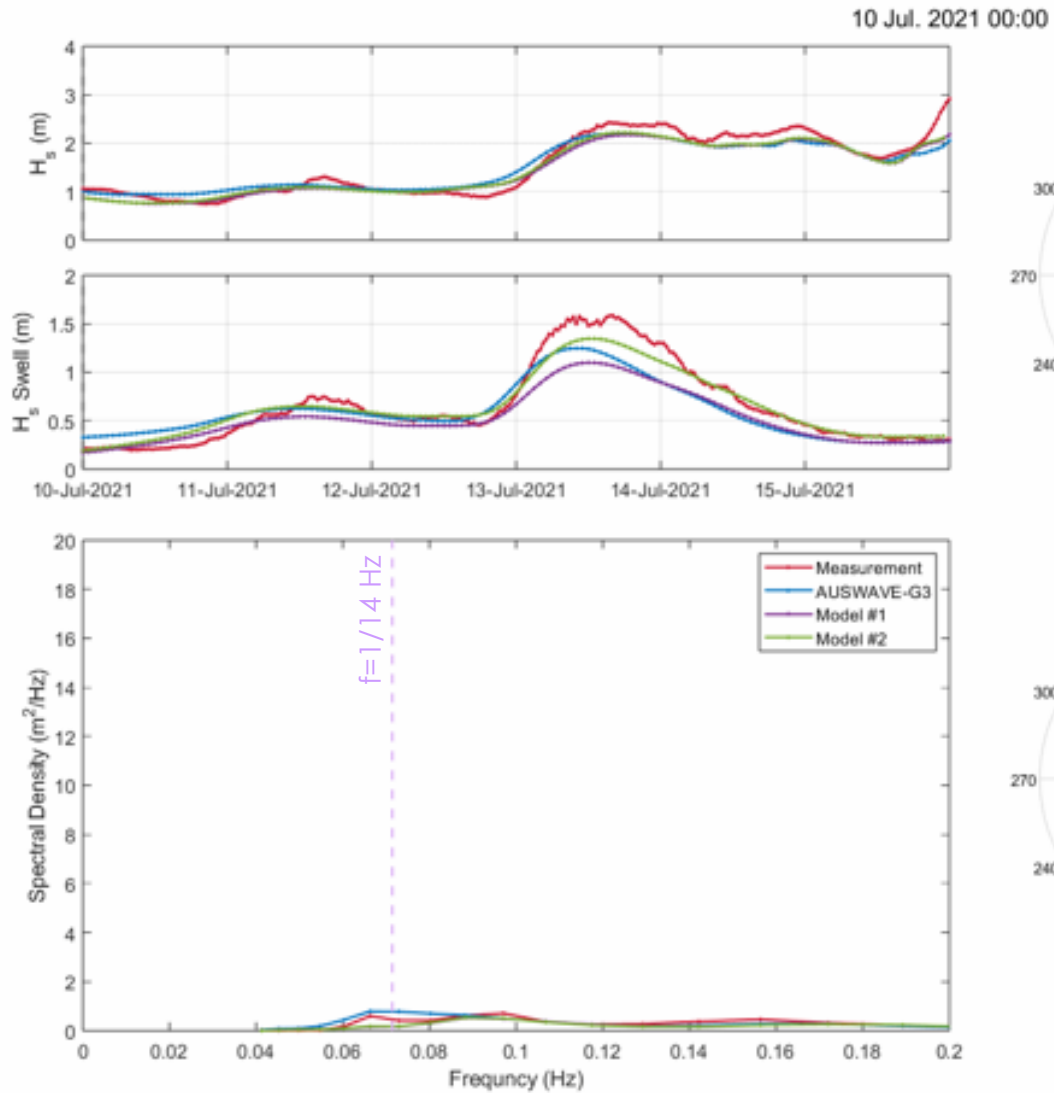
# Assessment of AUSWAVE-G3



08 Jul. 2021 00:00



# Assessment of AUSWAVE-G3



**Model #1:** Same as AUSWAVE-G3 with ECMWF winds and Copernicus currents.

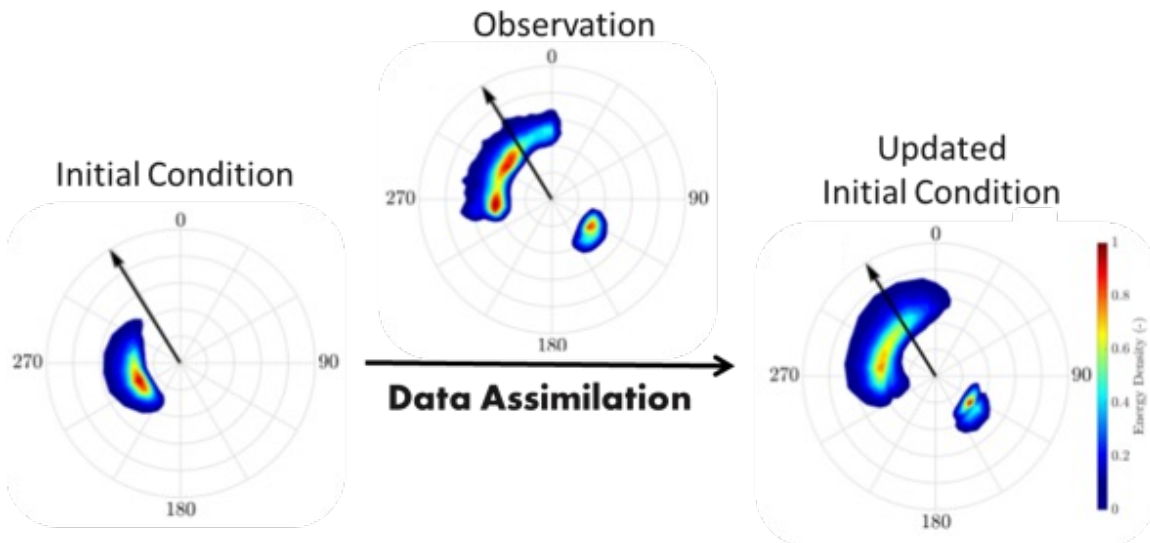
**Model #2:** Same as Model #1 with increased spectral resolution ( $8^\circ$  dirs. & 45 freq. bins).

# Data Assimilation in WaveWatch-III



**Approach 1)** Update the “Initial Condition”

**Approach 2)** Incorporate the DA scheme into the model



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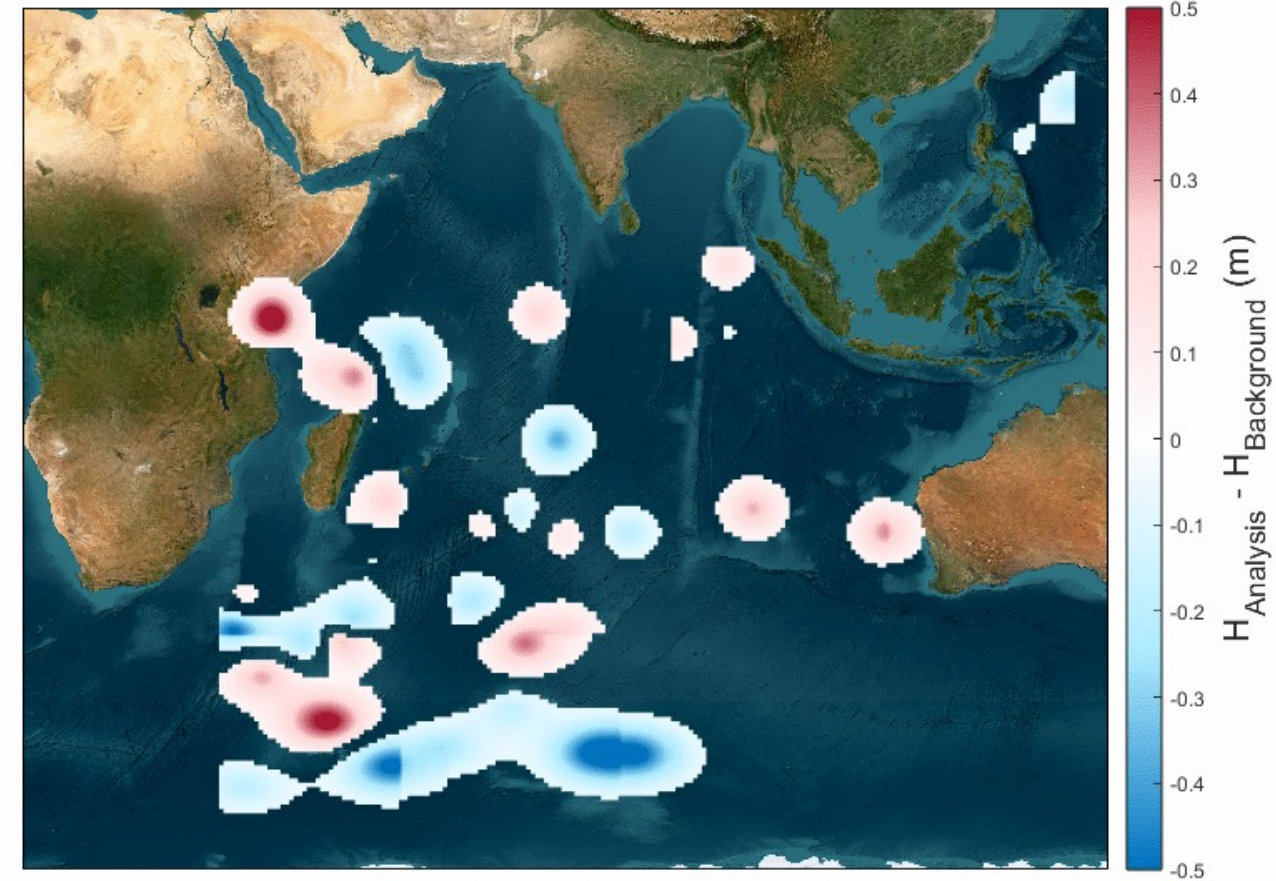
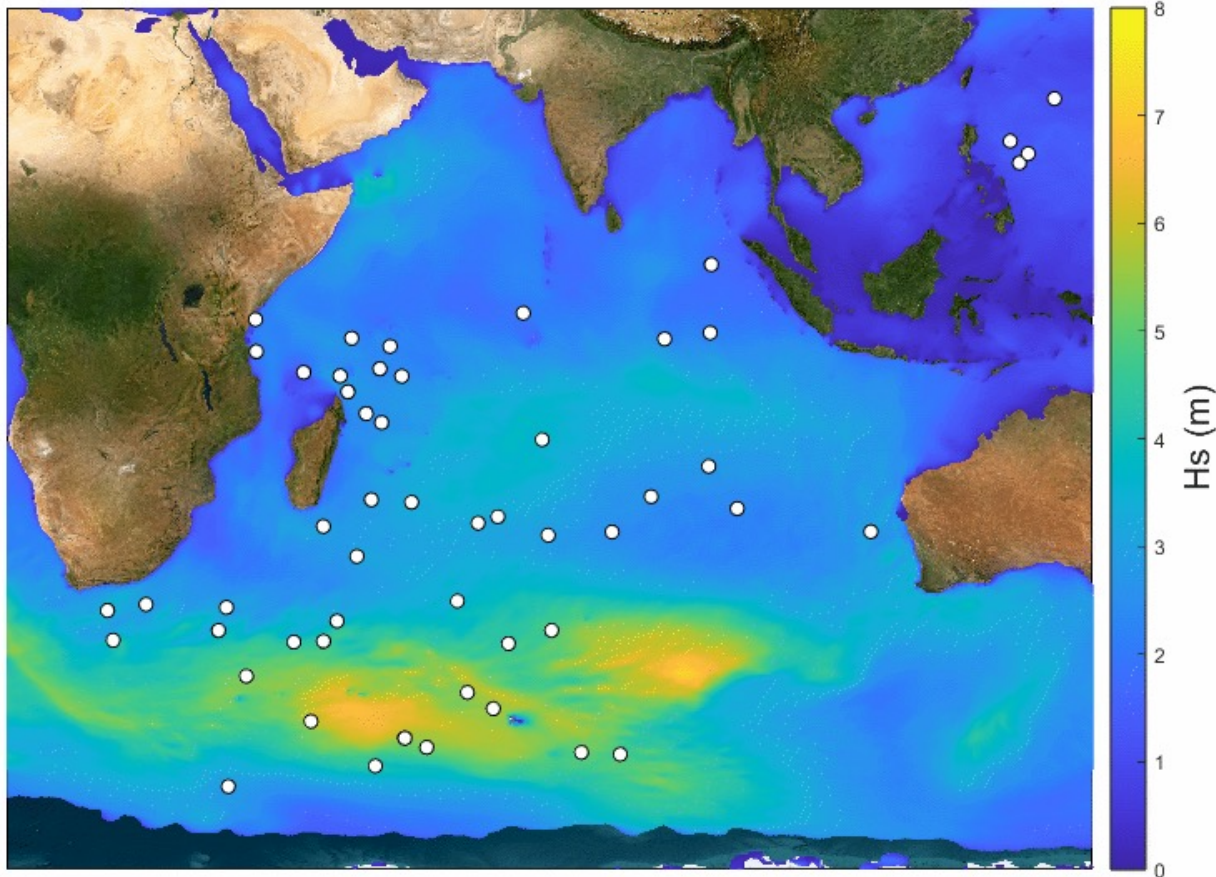
25
26 def check_db():
27     if not os.path.isfile(FILE_URI):
28         db.create_all()
29
30 @app.route("/")
31 def home():
32     check_db()
33     all_books = db.session.query(Book).all()
34     return render_template("index.html", books=all_books)
35
36 @app.route("/edit", methods=["GET", "POST"])
37 def edit():
38
39     if request.method == 'POST':
40         book_id = request.form["id"]
41         book_to_update = Book.query.get(book_id)
42         book_to_update.rating = request.form["rating"]
43         db.session.commit()
44         return redirect(url_for("home"))

```

# Assimilation of Hs

08 Jul. 2021 00:00

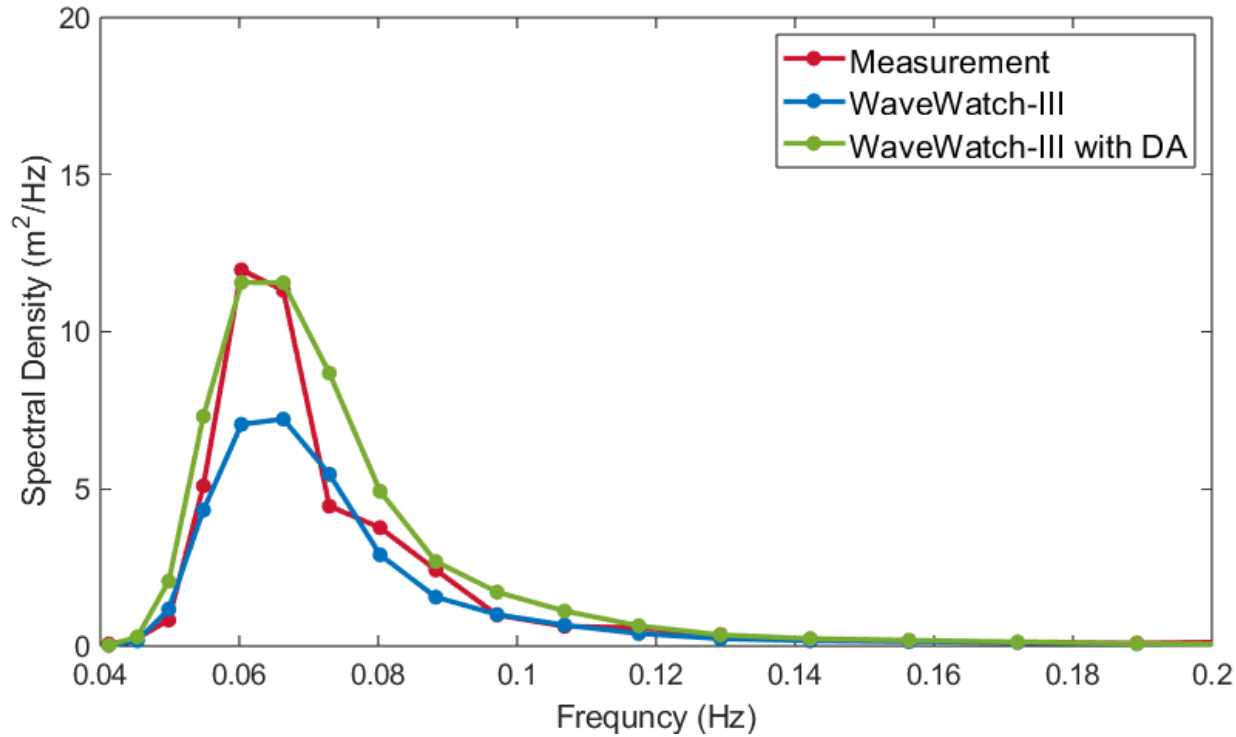
08 Jul. 2021 00:00



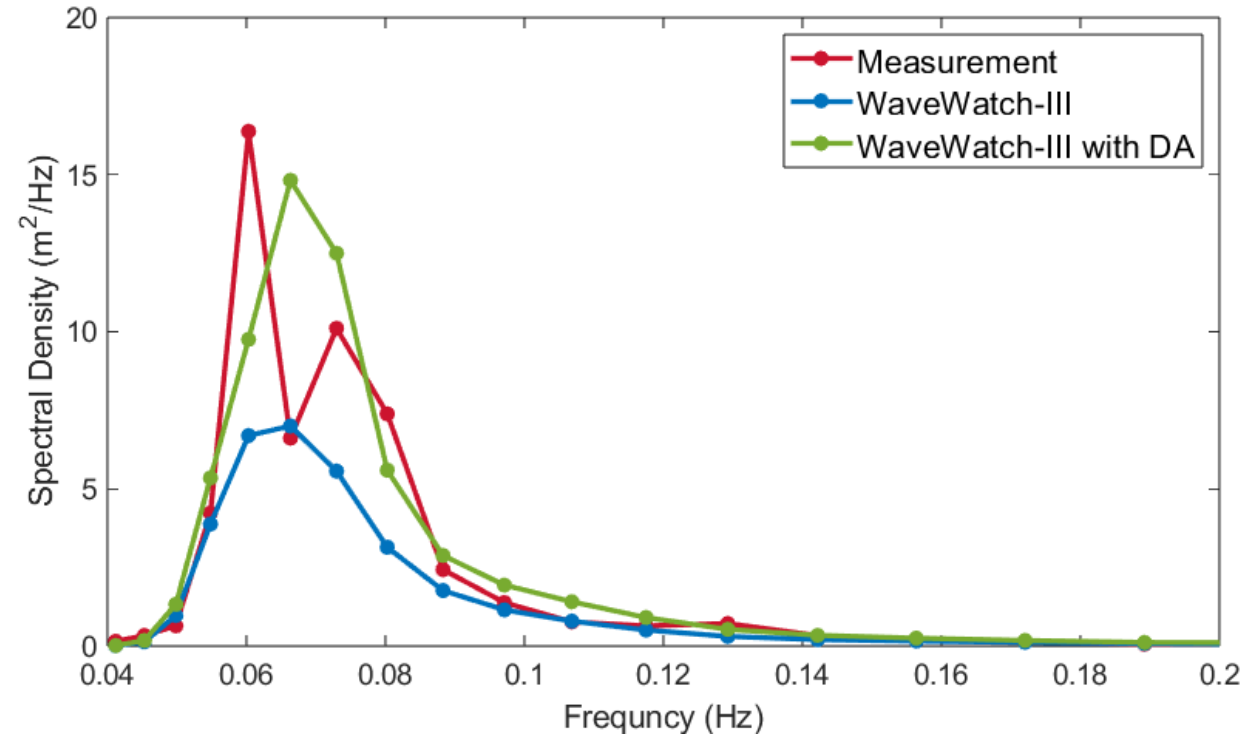
# Assimilation of Partitioned Hs



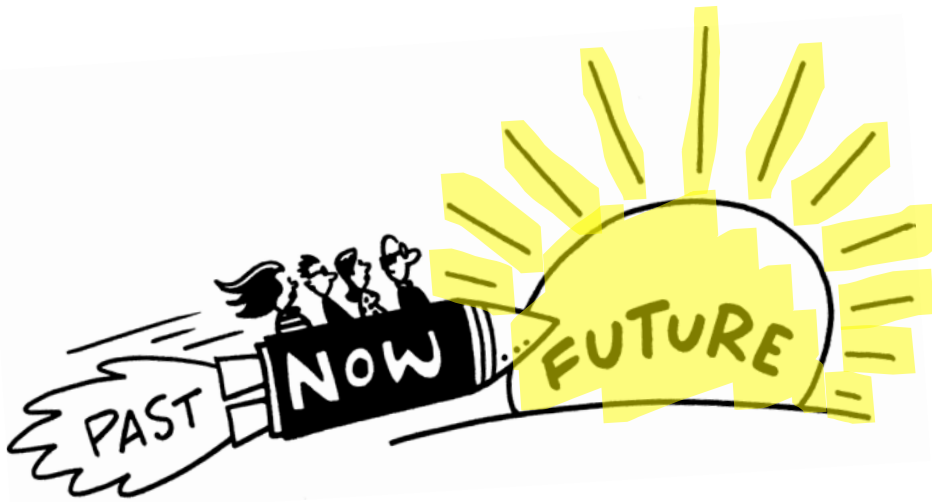
13 Jul 2021 13:00



13 Jul 2021 15:00

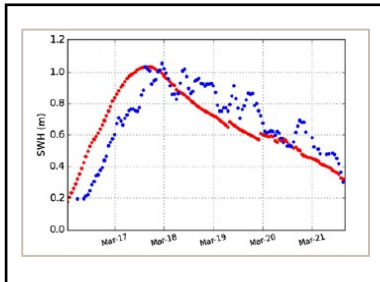


# Next Steps...

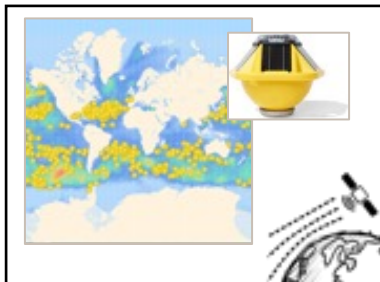


- Assimilation of observations in the spectral domain.
- Investigating alternative data assimilation techniques e.g., the Kalman Filter.
- Explore the model's performance with the assimilation of observations from various sources e.g., satellite.
- Improving the knowledge of the physical processes active in the swell propagation and decay.

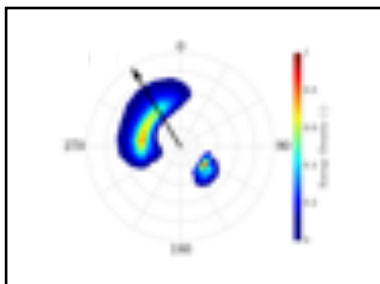
# Summary



Inaccuracies in swell predictions (e.g., arrival time) impact offshore operations, coastal protection measures, and climate models.



Increased availability of wave observations provide an opportunity for improved wave predictions through techniques such as DA.



DA techniques applied to wave models predominantly rely on bulk parameters while the ultimate gain is in spectral assimilation.





# Data Assimilation Methods



Data Assimilation

Variational  
3D VAR  
4D VAR

Sequential  
Optimal Interpolation  
Kalman Filter

Analysis Equation:

$$\mathbf{x}^a = \mathbf{x}^f + \mathbf{W} \overbrace{(\mathbf{y} - \mathbf{H}\mathbf{x}^f)}^{\text{Innovation}}$$

Kalman Gain:

$$\mathbf{W} = \mathbf{C}^f \mathbf{H}^T (\mathbf{H}\mathbf{C}^f \mathbf{H}^T + \mathbf{C}^o)^{-1}$$

Gaussian:

$$P(i, j) = \frac{V^f}{V^f + V^o} \exp\left(-\frac{(r_{ij})^2}{2L^2}\right)$$

2<sup>nd</sup> Order  
Autoregressive:

$$P(i, j) = \frac{V^f}{V^f + V^o} \left(1 + \frac{r_{ij}}{L}\right) \exp\left(\frac{-r_{ij}}{L}\right)$$